

# Search for $B_{s,d} \rightarrow \mu^+ \mu^-$ with CDF II

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April 26<sup>th</sup> 2012

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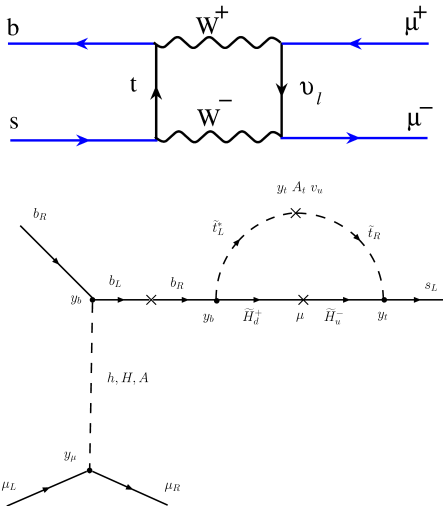
Argonne National Laboratory Seminar

PRL 107, 191801 (2011)  
PRD in preparation

## Introduction

# Motivation

- $B_s \rightarrow \mu^+ \mu^-$  can only occur through higher order FCNC diagrams in Standard Model (SM)
- Suppressed by the GIM Mechanism and helicity
- SM predicts very low rate with little SM background:  
 $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.2 \pm 0.2) \times 10^{-9}$   
 $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) = (1.0 \pm 0.1) \times 10^{-10}$   
 E.Gamiz et al. (HPQCD Collaboration), A.J. Buras et al.
- New Physics models predict enhancement
- Clean experimental signature



# Motivation: BSM prediction

- Large new contributions from models with new operators
- Modest enhancements without new operators
- Ratio of  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$  and  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$  is important to discriminate amongst BSM models
- Correlation between CP violating phase in  $B_s \rightarrow J/\psi \phi$  and  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$

Model	$\mathcal{B}(B_{s,d} \rightarrow \mu^+ \mu^-)$ Enhance
MFV	1000%
CMFV	20%
LHT	30%
RS	10%
4G	250%
AC	1000%
RVV	1000%

**Table:** Maximal enhancements for  $\mathcal{B}(B_{s,d} \rightarrow \mu^+ \mu^-)$  from different theoretical NP models. SUSY Models: MFV=Minimal Flavor Violation; AC=Agashe, Carone; RVV=Ross, Velasco-Sevilla, Vives. [Plenary talk, A.Buras, Beauty 2011](#)

**Powerful tool in NP model discrimination**

# Analysis Description

## Simple Analysis

- 2 Muons low  $p_T$  muons ( $p_T < 15 \text{ GeV}/c$ )
- Identify methods of suppressing background and keep signal
- Look for bump in di-muon mass distribution

## Analysis Strategy

- Blind ourselves to di-muon signal mass region
- Use mass sidebands to estimate dominant background in signal region
- Optimize selection criteria a priori
- Build confidence in background estimates by employing same methods on control regions
- Unblind and perform statistical analysis of result

# Analysis Properties and Techniques

## Analysis Properties

- $b$  Physics analysis, good MC modeling of  $b$  and  $c$  hadrons
- CDF is well understood detector
- Large data set ( $\sim 10\text{fb}^{-1}$ )
- Previous iterations of the analysis
- Mature calibrations

## Analysis Techniques

- Use normalization to measure  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$
- Multi-variate analysis
- Control regions for background check
- Statistical interpretation: CLs limits, p-values,  $\Delta\chi^2$  fit

# Signal vs. Background

## Signal Properties

- Final state fully reconstructed
- $B_s$  is long lived ( $c\tau \approx 450\mu\text{m}$ )
- B fragmentation is hard: few additional tracks

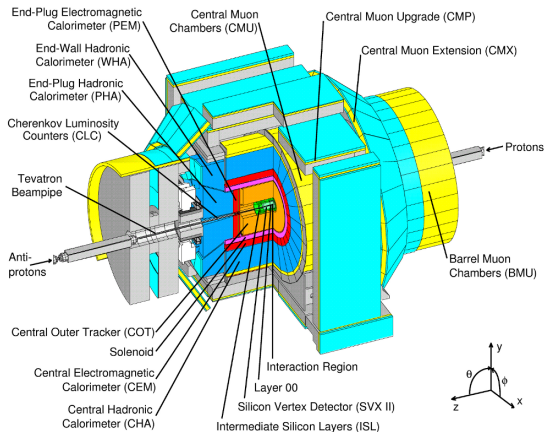


## Background contributions & characteristics

- Sequential semi-leptonic decay:  $b \rightarrow c\mu^-X \rightarrow \mu^+\mu^-X$
- Double semi-leptonic decay:  $bb \rightarrow \mu^-\mu^+X$
- Continuum  $\mu^-\mu^+$
- $\mu$  + fake and fake+fake
  - Partially reconstructed
  - Softer
  - Short lived
  - Has more tracks
- $B \rightarrow h^+h'^-$ : peaking in signal region ( $h$  and  $h'$  are pions or kaons)

# CDF II Detector

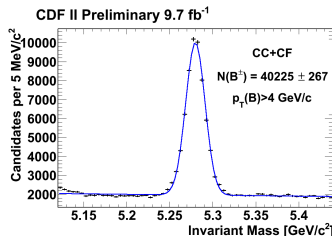
- Multi-purpose detector
- Silicon vertex detector close to beam line  $\Rightarrow 35 \mu\text{m}$  vertex resolution
- Central Outer Tracker (COT)  $\Rightarrow$  multi-wire drift chamber
- Good Muon drift chambers: Central and some Forward (yellow and cyan)
- Use entire Run II data set





# What do we measure?

- Measure rate of  $B_s \rightarrow \mu^+ \mu^-$  relative to  $B^+ \rightarrow J/\psi K^+$ ,  $J/\psi \rightarrow \mu^+ \mu^-$
- Apply same selection to find  $B^+ \rightarrow J/\psi K^+$
- Systematic uncertainties will cancel in ratio



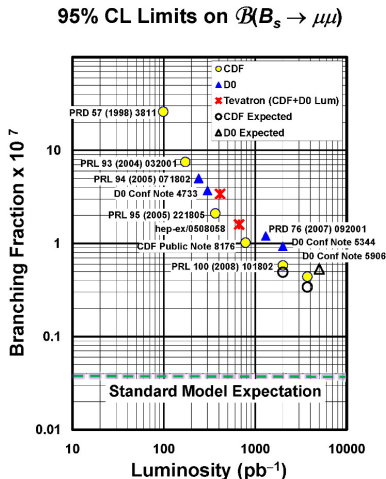
$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = N_{B_s} \cdot \left( \frac{1}{N_{B^+}} \frac{\epsilon_{B^+}^{\text{trig}}}{\epsilon_{B_s}^{\text{trig}}} \right) \cdot \left( \frac{\epsilon_{B^+}^{\text{reco}}}{\epsilon_{B_s}^{\text{reco}}} \frac{\alpha_{B^+}}{\alpha_{B_s}} \frac{1}{\epsilon_{NN}^{NN}} \right) \cdot \left( \frac{f_u}{f_s} \cdot \mathcal{B}(B^+ \rightarrow J/\psi K^+ \rightarrow \mu^+ \mu^- K^+) \right)$$

From Data, From MC, From PDG

$$\begin{aligned} N_{B^+} &\sim 2 \times 10^4, \quad \frac{\epsilon_{B^+}^{\text{trig}}}{\epsilon_{B_s}^{\text{trig}}} \sim 1 \\ \frac{\epsilon_{B^+}^{\text{reco}}}{\epsilon_{B_s}^{\text{reco}}} &\sim 1, \quad \frac{\alpha_{B^+}}{\alpha_{B_s}} \sim 0.5, \quad \frac{1}{\epsilon_{NN}^{NN}} \sim 1 \\ \frac{f_u}{f_s} &\sim 3, \quad \mathcal{B}(B^+ \rightarrow J/\psi K^+ \rightarrow \mu^+ \mu^- K^+) \sim 5 \times 10^{-5} \end{aligned}$$

# History of Limits

- Iterations of analysis before 2011
- CDF and D0 set upper limits on  $B_s \rightarrow \mu^+ \mu^-$
- Tightest limit from CDF with 3.7  $\text{fb}^{-1}$  of data:  
 $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 4.3 \times 10^{-8}$  and  
 $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 7.6 \times 10^{-9}$  at  
95% C.L.



Already greatly constrained NP parameter space  
Closing on SM prediction (factor  $\sim 10$ )

# Analysis Improvements after $3.7 \text{ fb}^{-1}$ Iteration\*

- Increased acceptance by including more forward detector regions ( $\sim 7\%$ )
- More than double the data set
- New multi-variate discriminant (NeuroBayes)
- New calibration for muon ID
- New background estimates
- Additional Statistical Interpretation

## Event Selection

## Central-Central (CC)

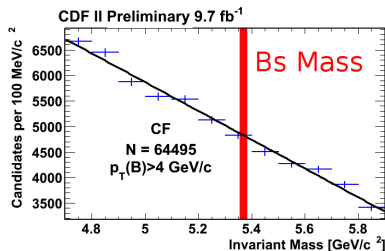
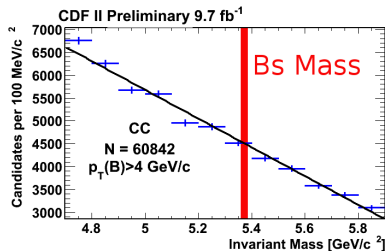
- 2 Muons with  $|\eta| < 0.6$
- $p_T > 1.5 \text{ GeV}/c$  or  $p_T > 3.0 \text{ GeV}/c \rightarrow$  Range out
- Muons must be separated by  $\Delta\phi_{SL6} > 1.25^\circ \rightarrow$  tracking/muon stub granularity

## Central-Forward (CF)

- Muon with  $|\eta| < 0.6$  and muon with  $0.6 < |\eta| < 1.0$
- $p_T > 2.0 \text{ GeV}/c \rightarrow$  Range out
- Opposite sign muons
- $|\Delta z_0| < 5 \text{ cm} \rightarrow$  Should come from same source

# Baseline Requirements

- $p_T(\mu) > 2.0(2.2) \text{ GeV}/c \rightarrow$  **Rapidly changing trigger eff**
- $p_T(B_s) > 4.0 \text{ GeV}/c$
- Hits in 3 layers of SVX  $\rightarrow$  **Improved impact parameter resolution**
- Muon likelihood and  $dE/dx \rightarrow$  **Kaon rejection**
- Vertex: Proper decay length,  $\chi^2$  of vertex, etc  $\rightarrow$  **Reject short lived background**
- Invariant mass
- Isolation and Pointing angle  $\rightarrow$  **Reject jets and short lived**
  - Isolation =  $\frac{p_T(\mu\mu)}{\Sigma p_T(\text{other tracks}) + p_T(\mu\mu)}$  in  $R=1.0$   $\eta - \phi$  cone.
  - Pointing angle = angle between di-muon momentum vector and vector pointing from primary to secondary vertex

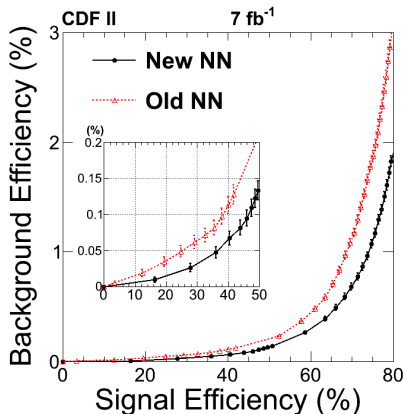


# New Neural Network

- New 14-variable NN to increase S/B
  - Studied different input variables
- Carefully chose input variables to avoid bias in  $M_{\mu\mu}$
- Twice the background rejection as old NN

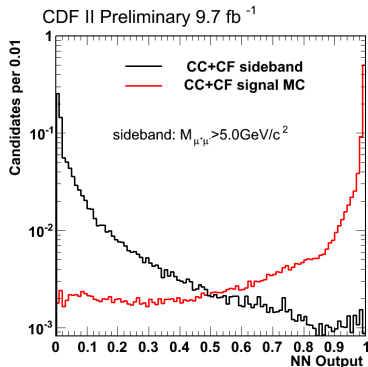
## NN Input Variables

- $\lambda$  (proper decay length)
- Isolation
- Pointing angle
- $\lambda/\sigma_\lambda$
- lower  $p_T(\mu)$
- Secondary vertex  $\chi^2$
- Decay length ( $L_{3D}$ )
- Transverse Decay length significance ( $L_{xy}/\sigma_{L_{xy}}$ )
- 2D Pointing angle
- Smaller impact parameter
- Larger impact parameter
- Smaller impact parameter significance
- Larger impact parameter significance
- $B_{s(d)}$  impact parameter



# Neural Network Training

- Signal training sample:  $B_s \rightarrow \mu^+ \mu^-$  MC
- Background sample: di-muon mass sideband for combinatorial background rejection
- Separate NN's for CC and CF
- Investigated 20 input variables
- Excluded variables that caused di-muon mass/NN output correlation
  - Opening angle between muons
  - $p_T(B_s)$
- Final NN used 14 strongest separating variables
- Combined separation power into 1 output that ranges between 0 and 1



## NN Signal Region

- Chose  $\text{NN} > 0.7$
- Divided region into 8 NN bins based on expected limit optimization



# Signal Efficiencies

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = N_{B_s} \cdot \frac{1}{N_{B^+}} \cdot \left( \frac{\epsilon_{B^+}^{trig}}{\epsilon_{B_s}^{trig}} \cdot \frac{\epsilon_{B^+}^{reco}}{\epsilon_{B_s}^{reco}} \cdot \frac{\alpha_{B^+}}{\alpha_{B_s}} \cdot \frac{1}{\epsilon_{B_s}^{NN}} \right) \cdot \frac{f_{\mu}}{f_s} \cdot \mathcal{B}(B^+ \rightarrow J/\psi K^+ \rightarrow \mu^+ \mu^- K^+)$$

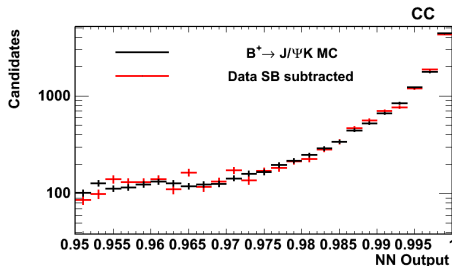
- Estimate total acceptance and efficiency
- Estimate separately for  $B_s \rightarrow \mu^+ \mu^-$  and  $B^+ \rightarrow J/\psi K^+$ 
  - Kinematic differences in 2 and 3 body decays

## Acceptance and Efficiency Broken Down

- $\alpha_{B_s}$ : Geometric and kinematic acceptance of trigger  $\rightarrow$  estimated with MC
- $\epsilon_{B_s}^{trig}$ : Trigger efficiency within acceptance  $\rightarrow$  measured in data
- $\epsilon_{B_s}^{reco}$ : Efficiency of baseline requirements for event passing trigger  $\rightarrow$  estimated with data and MC
- $\epsilon^{NN}$ : Efficiency for each NN bin ( $B_s$  only)  $\rightarrow$  estimated with MC

# NN Efficiency\*

- Estimated using  $B_s \rightarrow \mu^+ \mu^-$  MC
- Estimated for 8 NN bins
- Highest NN bin accounts for majority of sensitivity (46% efficiency)



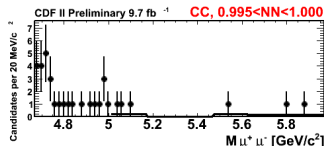
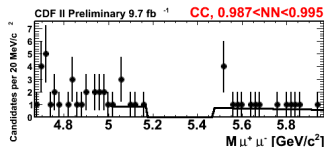
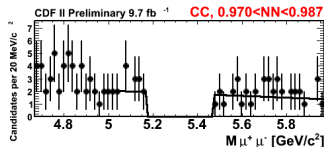
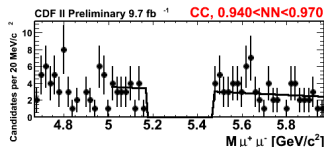
## Systematics

- Apply NN to  $B^+ \rightarrow J/\psi K^+$  MC and data and compare efficiencies
- Overall  $\sim 5\%$  shift between MC and data
- Applied as systematic to highest NN bin
- Additional 4% systematic applied based on the iso and  $p_T(B)$  MC mismodeling

## Background Estimation

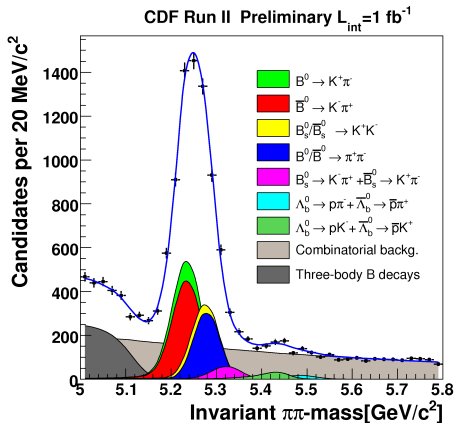
# Combinatorial Background Estimates

- Exclude  $M_{\mu^+\mu^-} < 5.0 \text{ GeV}/c^2$  region, enhanced with  $B \rightarrow \mu^+\mu^- X$  decays
- Fit first order polynomial to sidebands in each NN bin
- Estimate systematics due to shape uncertainty by fitting alternative function
  - Only for highest 3 NN bins
- Expect  $\sim 1$  background event in CC channel and  $\sim 3$  in CF channel for the highest NN bin



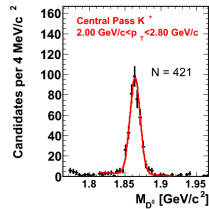
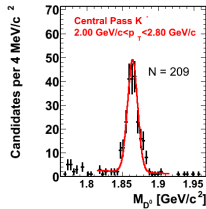
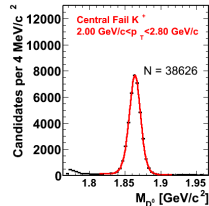
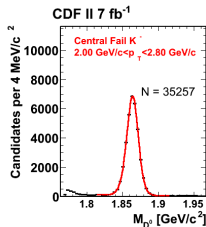
# Peaking Background Estimates\*

- Only significant peaking background is  $B \rightarrow h^+ h'^- (h \text{ is hadron})$
- Background from  $\Lambda_b$  decays much lower
  - Smaller production rates
  - Protons are significantly rejected by muon ID
- Estimated using MC and  $D^*$ -tagged  $D^0 \rightarrow \pi^+ K^-$  data
  - MC for  $p_T$  and mass distributions
  - $D^*$ -tagged  $D^0 \rightarrow \pi^+ K^-$  data to assess rate at which pions/kaons fake muons
- More in  $B_d$  due to muon mass hypothesis



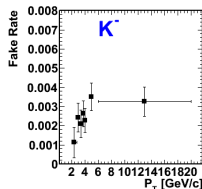
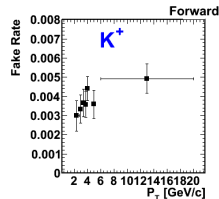
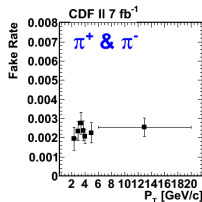
# Data Set for Peaking Background\*

- Need to assess how often a kaon or pion passes muon reconstruction
- Use  $D^*$ -tagged  $D^0 \rightarrow \pi^+ K^-$  data  $\Rightarrow$  very pure samples of kaons and pions
- Sample collected with Two Track Trigger
- Numerator: Pass dE/dx and muon likelihood requirement
- Extract yield using Gaussian+pol fit



# Fake Rate Parametrization\*

- Separate fake rates for  $\pi^\pm$ ,  $K^+$ , and  $K^-$
- Parametrized in  $p_T \Rightarrow$  Higher momentum, more punch through
- Found inst. lumi dependence  $\Rightarrow$  estimated fake rate in 4 lumi bins
  - Fake rates changed by 20% to a factor of 3 due to lumi
- Applied fake rates as weights to  $D^*$  data and compared to actual number of fakes  $\Rightarrow$  Difference assigned as systematic.



# Background Estimate Check

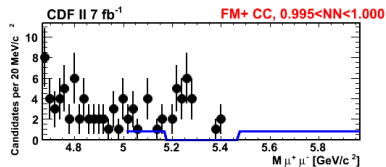
- Check background estimates with background dominated control samples
  - Signal has two opposite sign muons with positive lifetime
  - Control samples have opposite sign negative lifetime, same-sign positive/negative lifetime, and reverse muon ID
  - Total of 64 samples
- Apply same background methods on control sample that we can unblind

NN cut	pred	obsv	prob(%)
$0.700 < NN < 0.760$	$268.8 \pm (14.3)$	249	82.3
$0.760 < NN < 0.850$	$320.8 \pm (16.1)$	282	95.1
$0.850 < NN < 0.900$	$150.3 \pm (9.9)$	156	36.5
$0.900 < NN < 0.940$	$146.2 \pm (9.7)$	158	23.0
$0.940 < NN < 0.970$	$146.2 \pm (9.7)$	137	72.9
$0.970 < NN < 0.987$	$100.4 \pm (7.8)$	98	58.3
$0.987 < NN < 0.995$	$78.8 \pm (6.8)$	59	97.0
$0.995 < NN < 1.000$	$41.2 \pm (4.8)$	42	47.2



# $B \rightarrow hh$ Background Check\*

- Used control sample with reversed muon ID cuts: enhanced in hadrons
  - Total of 16 samples
- Estimated fake rates for this sample using  $D^*$ -tagged for fake rate: Ratio of pions/kaons failing muon ID



## Conclusion

- Checked combinatorial and peaking background estimates with control samples
- Good agreement between predicted and observed

# Expected Sensitivity

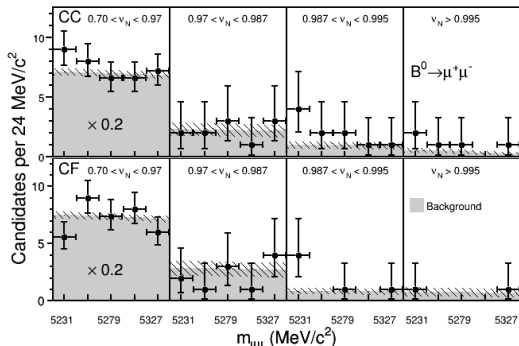
$B_s \rightarrow \mu^+ \mu^-$  CC

NN Bin	$\epsilon_{NN}$	$B \rightarrow hh$ Bkg	Total Bkg	Exp SM Signal
$0.700 < NN < 0.970$	20%	0.05	$169.29 \pm 6.29$	$0.32 \pm 0.06$
$0.970 < NN < 0.987$	8%	0.02	$7.91 \pm 1.85$	$0.13 \pm 0.02$
$0.987 < NN < 0.995$	12%	0.03	$3.95 \pm 1.28$	$0.20 \pm 0.04$
$0.995 < NN < 1.000$	46%	0.11	$0.79 \pm 0.70$	$0.75 \pm 0.13$

- $\sim 80\%$  signal efficiency for NN
- Small contribution of peaking background compared to combinatorial ( $B_s$ )
- Expect  $\sim 2$  SM signal event (CC and CF)

## $B_d$ Results

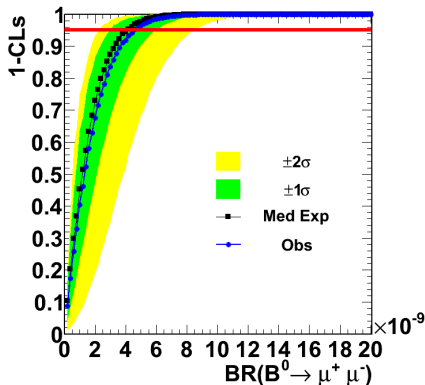
# Comparison of observation and background estimates



- Five mass bins
- Five lowest NN bins combined
- Light gray: Background estimates, Hashed: Systematic errors on background
- Error bars on points: Poisson error on mean
- **No excess in  $B_d$  mass region**

# CLs Bounds for $B_d$

- Generate background only pseudo data and  $s + b$  pseudo data for many BR
- CLb = p-value using background-only pseudo data
- CLs+b = p-value using  $s + b$  pseudo data
- CLs = CLs+b/CLb, exclude if  $1 - \text{CLs} > 95\%$

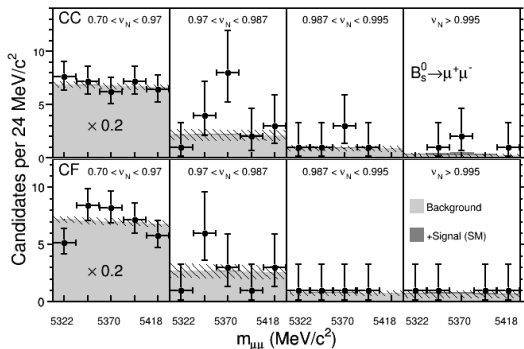


## Results

- Observed:  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 4.6 \times 10^{-9}$  @ 95% C.L.
- Expected  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 4.0 \times 10^{-9}$  @ 95% C.L.
- SM prediction:  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) = (1.0 \pm 0.1) \times 10^{-10}$

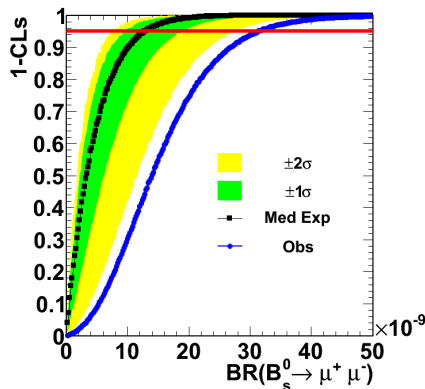
## $B_s$ Results

# Comparison of observation and background estimates



- Dark gray: Expected SM signal
- **Excess over background-only in central region (the most sensitive)**

# CLs Bounds for $B_s$



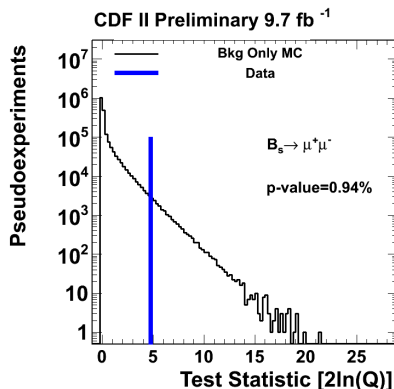
## Results

- Observed:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 3.1 \times 10^{-8}$  @ 95% C.L.
- Expected:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 1.3 \times 10^{-8}$  @ 95% C.L.  $\rightarrow > 2\sigma$  deviation
- SM Predicted:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.2 \pm 0.2) \times 10^{-9}$



# p-Value Determination

- Construct likelihood function ( $\mathcal{L}$ ):  
Product of 80 Poisson PDF's
- Considered 3 hypotheses
  - background-only,  $\mathcal{L}(b)$ ,  $b$  from total background estimates
  - signal+background,  $\mathcal{L}(s+b)$ ,  $s$  is floating
  - SM+background,  $\mathcal{L}(\text{SM}+b)$ , from SM  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$
- Constructed log likelihood ratio:  
 $2\ln(Q)$  with  $Q = \frac{\mathcal{L}(s+b|\text{data})}{\mathcal{L}(b|\text{data})}$
- Generate pseudo-data while varying nuisance parameters
  - Systematics included as nuisance parameters modeled as Gaussians

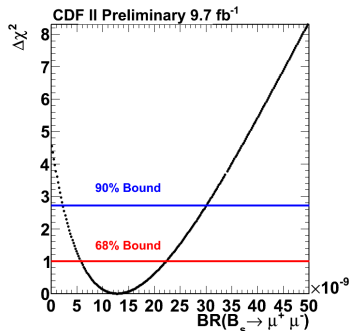


## Results

- $B_s$  bkg-only p-value: 0.94%
- $B_s$  SM+bkg p-value: 7.1%
- ( $B_d$  bkg-only p-value: 41%)

# $B_s$ : Central Values, Bounds and P-Values

- Includes all systematics
- 90% Bound:  
 $2.2 \times 10^{-9} < \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 3.0 \times 10^{-8}$
- Stable: No large deviation when only using subset of bins



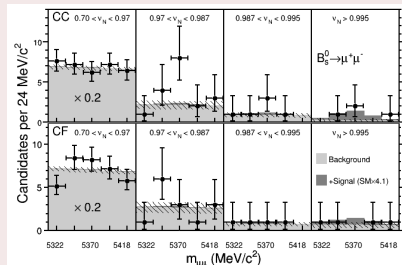
## Summary of p-values and limits

	All Bins	2 Highest NN Bins
<b>Best Fit (<math>\times 10^{-8}</math>)</b>	$1.3^{+0.9}_{-0.7}$	$1.0^{+0.8}_{-0.6}$
<b>90% Bounds (<math>\times 10^{-8}</math>)</b>	$0.22 < \mathcal{B} < 3.0$	$0.08 < \mathcal{B} < 2.5$
<b>Bkg Only p-value</b>	0.94%	2.1%
<b>SM+Bkg p-value</b>	7.1%	22.5%

# Third NN Bin Excess

## Background Estimate Problem?

- Combinatorial Background Problem
  - $B_d$  Uses same sideband as  $B_s \Rightarrow$  No excess in  $B_d$
- Peaking Background Problem
  - Only peaking background is  $B \rightarrow hh$
  - 10x larger in  $B_d$  region
  - No excess in  $B_d \Rightarrow$  good fake rates

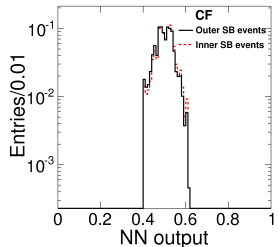
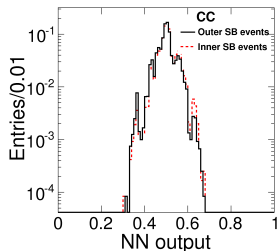


## Neural Network Problem?

- Mass bias?  $\Rightarrow$  Many studies show no bias
- Over-trained?  $\Rightarrow$  Compared NN with different training sample, no difference
- Mismodels data?  $\Rightarrow$  No difference between MC and data in normalization mode

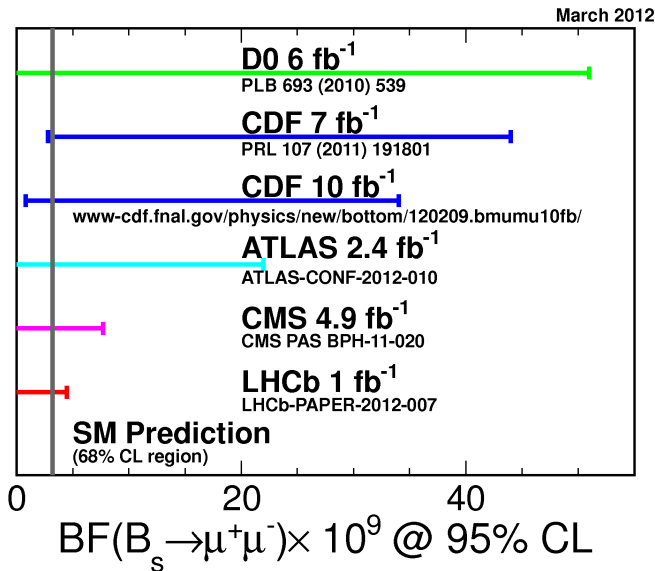
# NN Mass Correlation Studies: NN inner/outer SB training

- Defined inner sideband close to signal region, and outer sideband
- Trained NN using inner sideband as signal and outer as background sample
- Inner and outer sideband regions are kinematically similar, di-muon mass is main difference
- Tests whether NN is selecting events based on di-muon mass



**Conclusion: No difference in NN output for inner and outer after training**  
**Mass bias unlikely to be cause of excess in 3rd NN bin of CC**

# Current Experimental Status



# Summary

- New  $B_s \rightarrow \mu^+ \mu^-$  search with full CDF Run II data set
  - First CDF result using full Run II data set
- $0.8 \times 10^{-9} < \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 3.4 \times 10^{-8}$  @ 95% C.L.
  - First two sided bound
- $B_d \rightarrow \mu^+ \mu^- < 4.6 \times 10^{-9}$  @ 95% C.L.
- PRD manuscript in preparation
- Many exciting new results from LHC
- Final CDF  $B_s \rightarrow \mu^+ \mu^-$  result
  - Tevatron Run II+CDF II+ingenuity provided 2 orders of magnitude improvement in sensitivity

# x-Ray Beam Size Monitor

# Intro to CESR-TA and xBSM

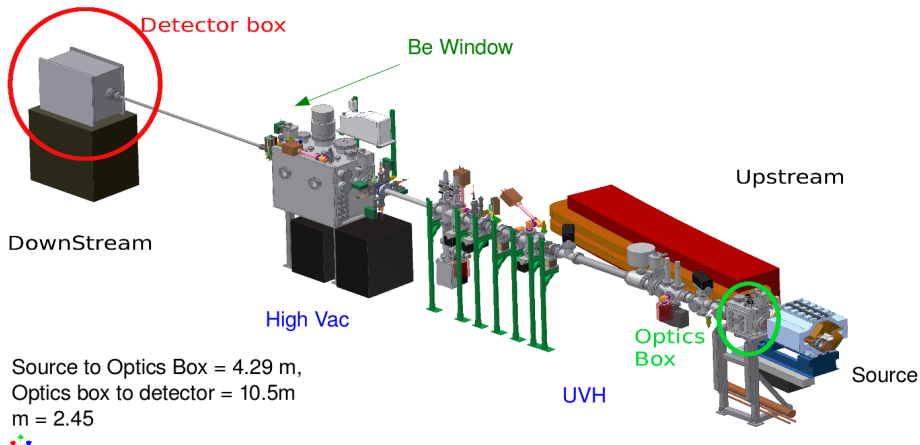
- Cornell Electron-positron Storage Ring Test Accelerator
- Test accelerator for cooling rings for ILC
- 14 ns bunch spacing

## xBSM

- Need feedback from methods of reducing bunch size
- Measure bunch size every 14 ns using synchrotron x-rays

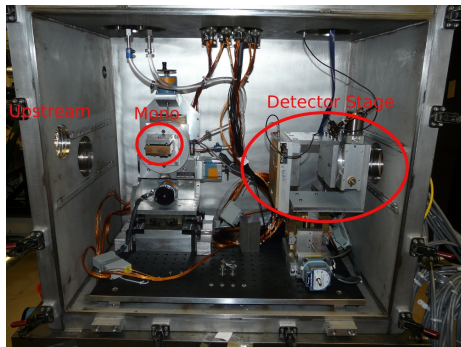


# x-Ray Beam Line



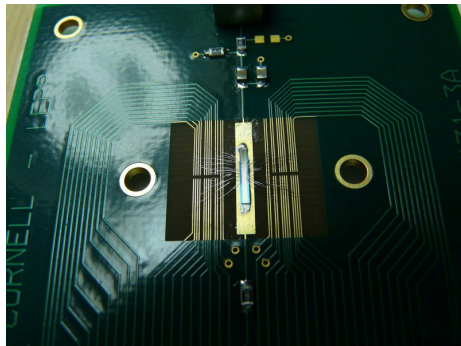
# Beam Size Measurement

- 1D vertical beam size measurement
- Optics Elements: Pinhole, Fresnel Zone Plate, Coded Aperture
- Magnification of  $\sim 2.5$
- Use monochromator to select small range in wave lengths
- Detector in vacuum, 10 m away from optics
  - Detector consists of 32 GaAs diodes in vertical orientation (measure 1D bunch size)
  - Can do integrated slow readout with each diode by moving motors
  - Snapshot readout: readout all 32 diodes every 14 ns



# New Detector

- 32 diode GaAs
- New detector board (detector wire bonded)
  - Tested several detectors from vendors
  - Redesigned detector board for optimum wire bonding
- Commissioned new detector
  - Wrote new detector read out software
  - Read out mapping (diode number to physical location)
  - Gain calibration



# xBSM Conclusion

## Started with

- Integrated read out of one diode (moving the diode through beam)
- Positron read out only

## After one year

- Selected 32 diode array and designed new detector board
- Automated diode mapping
- Gain calibration method established
- Successful beam profile for each 14 ns bunch
- Automatic 14 ns beam size reporting
- Started construction of electron beam size setup